**ST. FRANCIS INSTITUTE OF TECHNOLOGY**

**DEPARTMENT OF INFORMATION TECHNOLOGY**

**SECURITY LAB**

**Experiment – 4: Implementation of RSA cryptosystem**

**Aim:** Write a program to implement and analyze RSA cryptosystem.

**Objective:** After performing the experiment, the students will be able to understand the encryption and decryption using RSA cryptosystem.

**Lab objective mapped:**

L502.2: Students should be able to Analyse and implement public key algorithms like RSA

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**Prerequisite:** Basic knowledge of RSA algorithm.

**Requirements:** PYTHON

**Pre-Experiment Theory:**

RSA was invented by Ron Rivest, Adi Shamir, and Len Adleman and hence, it is termed as RSA cryptosystem. We will see two aspects of the RSA cryptosystem, firstly generation of key pair and secondly encryption-decryption algorithms.

**Generation of RSA Key Pair**

Each person or a party who desires to participate in communication using encryption needs to generate a pair of keys, namely public key and private key. The process followed in the generation of keys is described below −

1. Generate the RSA modulus (n)
   1. Select two large primes, p and q.
   2. Calculate n=p×q( For strong unbreakable encryption, let n be a large number, typically a minimum of 512 bits.)
2. Find Derived Number (e)
   1. Number e must be greater than 1 and less than ϕ(n) = (p − 1)(q − 1).
   2. There must be no common factor for e and ϕ(n) except for 1. In other words two numbers e and ϕ(n) are co-prime.
3. Form the public key
   1. The pair of numbers (e, n) form the RSA public key and is made public.
   2. Interestingly, though n is part of the public key, difficulty in factorizing a large prime number ensures that attacker cannot find in finite time the two primes (p & q) used to obtain n. This is strength of RSA.
4. Generate the private key
5. Private Key d is calculated from p, q, and e. For given n and e, there is unique number d.
6. Number d is the inverse of e modulo ϕ(n). This means that d is the number less than ϕ(n) such that when multiplied by e, it is equal to 1 modulo ϕ(n)
7. This relationship is written mathematically as follows –

e×d = 1 mod ϕ(n)

The Extended Euclidean Algorithm takes p, q, and e as input and gives d as output.

**Encryption and Decryption**

Once the key pair has been generated, the process of encryption and decryption are relatively straightforward and computationally easy.

**RSA Encryption**

* Suppose the sender wish to send some text message to someone whose public key is (e,n).
* The sender then represents the plaintext as a series of numbers less than n.
* To encrypt the first plaintext P, which is a number modulo n. The encryption process is simple mathematical step as −

C = Pe mod n

* In other words, the ciphertext C is equal to the plaintext P multiplied by itself e times and then reduced modulo n. This means that C is also a number less than n.

**RSA Decryption**

* The decryption process for RSA is also very straightforward. Suppose that the receiver of public-key pair (e, n) has received a ciphertext C.
* Receiver raises C to the power of his private key d. The result modulo n will be the plaintext P.

Plaintext = Cd mod n

**Procedure:**

1. Write a program in python for key generation, encryption and decryption using RSA algorithm.
   1. For Key generation ask user to enter the value of prime numbers p & q and a public key ‘e’. (Note that values of p, q & e cannot be random, they should satisfy criteria as per RSA algorithm)
   2. Program should calculate private key element ‘d’ using Extended Euclidean Algorithm.
   3. Provide a set of public (e, n) and private key (d, n) as the output to the user.
   4. For RSA Encryption, ask user to enter the Message, and the public key. Provide Ciphertext as the output.
   5. For RSA Decryption, ask user to enter the ciphertext, and the private key. Provide retrieved message as the output.
2. Test the output of program for following Exercise:

**Exercise 1:** If party A and party B wish to use RSA to communicate securely. ‘A’ chooses public key (e, n) as (13, 77) and ‘B’ chooses public key (e, n) as (3, 33). Find

1. Value of prime numbers p, q, ϕ(n), public key for party A.
2. Calculate A’s Private key.
3. Value of prime numbers p, q, ϕ(n), public key for party B.
4. Calculate B’s Private Key.
5. What will be the cipher-text sent by A to B, if A wishes to send Message, M=5 to B.
6. Show how B will decrypt the message.
7. What will be the cipher-text sent by B to A, if B wishes to send M=3 to A.
8. Show how A will decrypt the message.

**Output:**

1. Attach the complete code performing key generation, encryption and decryption.
2. Attach the program output for key generation (display public key & private key), encryption and decryption of all the inputs given in exercise 1 and 2.

**Post Experimental Exercise (PEE):**

Solve Exercise 1 and 2 on journal sheets. [**Theoretical result and attached code’s output should match**].

**Exercise 2:** If party A and party B wish to use RSA to communicate securely. ‘A’ chooses public key (e, n) as (7, 247) and ‘B’ chooses public key (e, n) as (5, 221). Find

1. Value of prime numbers p, q, ϕ(n), public key for party A.
2. Calculate A’s Private key.
3. Value of prime numbers p, q, ϕ(n), public key for party B.
4. Calculate B’s Private Key.
5. What will be the cipher-text sent by A to B, if A wishes to send M=5 to B
6. Show how B will decrypt the message.
7. What will be the cipher-text sent by B to A, if B wishes to send M=3 to A
8. Show how A will decrypt the message.

**Conclusion:**

RSA is a strong encryption algorithm. RSA implements a public-key cryptosystem that allows secure communications and digital signatures, and its security rests in part on the difficulty of factoring large numbers.

**Code:**

from sympy import mod\_inverse

import math

# Function to factorize n into p and q

def factorize\_n(n):

for i in range(2, int(math.sqrt(n)) + 1):

if n % i == 0:

return i, n // i

raise ValueError("Failed to factorize n")

# Function to generate RSA parameters given public key (e, n)

def generate\_rsa\_params(e, n):

# Factorize n into p and q

p, q = factorize\_n(n)

# Compute φ(n)

phi = (p - 1) \* (q - 1)

# Compute the private key d

d = mod\_inverse(e, phi)

return p, q, phi, d

# Function to encrypt a message using RSA

def rsa\_encrypt(message, e, n):

return pow(message, e, n)

# Function to decrypt a message using RSA

def rsa\_decrypt(ciphertext, d, n):

return pow(ciphertext, d, n)

# Main execution

if \_\_name\_\_ == "\_\_main\_\_":

# User input for Party A's public key

e\_A, n\_A = map(int, input("Enter Party A's public key (e\_A, n\_A) separated by a space: ").split())

# User input for Party B's public key

e\_B, n\_B = map(int, input("Enter Party B's public key (e\_B, n\_B) separated by a space: ").split())

# Generate RSA parameters for Party A

p\_A, q\_A, phi\_A, d\_A = generate\_rsa\_params(e\_A, n\_A)

print(f"Party A's parameters:")

print(f"p\_A: {p\_A}")

print(f"q\_A: {q\_A}")

print(f"φ(n\_A): {phi\_A}")

print(f"Private key d\_A: {d\_A}")

# Generate RSA parameters for Party B

p\_B, q\_B, phi\_B, d\_B = generate\_rsa\_params(e\_B, n\_B)

print(f"Party B's parameters:")

print(f"p\_B: {p\_B}")

print(f"q\_B: {q\_B}")

print(f"φ(n\_B): {phi\_B}")

print(f"Private key d\_B: {d\_B}")

# Example encryption and decryption

# A sends message M = 5 to B

message\_from\_A = int(input("Enter the message M to be sent from A to B: "))

ciphertext\_A\_to\_B = rsa\_encrypt(message\_from\_A, e\_B, n\_B)

print(f"Ciphertext from A to B: {ciphertext\_A\_to\_B}")

# B decrypts the message

decrypted\_message\_B = rsa\_decrypt(ciphertext\_A\_to\_B, d\_B, n\_B)

print(f"Decrypted message received by B: {decrypted\_message\_B}")

# B sends message M = 3 to A

message\_from\_B = int(input("Enter the message M to be sent from B to A: "))

ciphertext\_B\_to\_A = rsa\_encrypt(message\_from\_B, e\_A, n\_A)

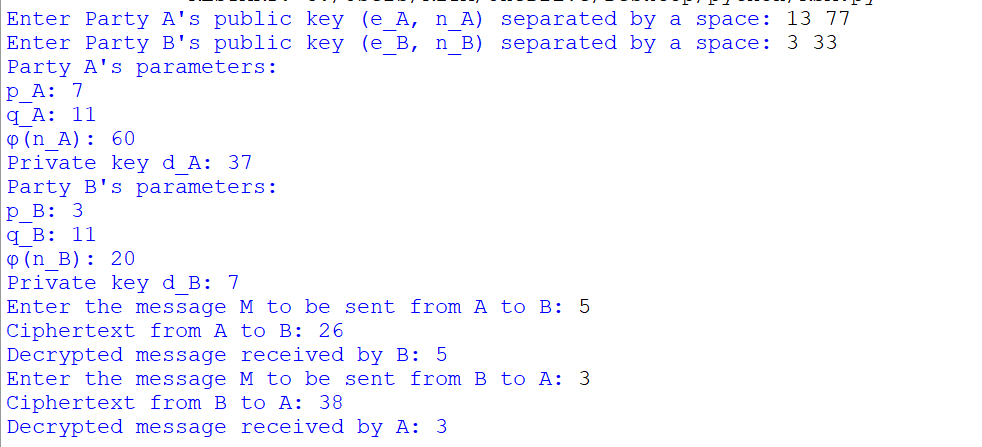
print(f"Ciphertext from B to A: {ciphertext\_B\_to\_A}")

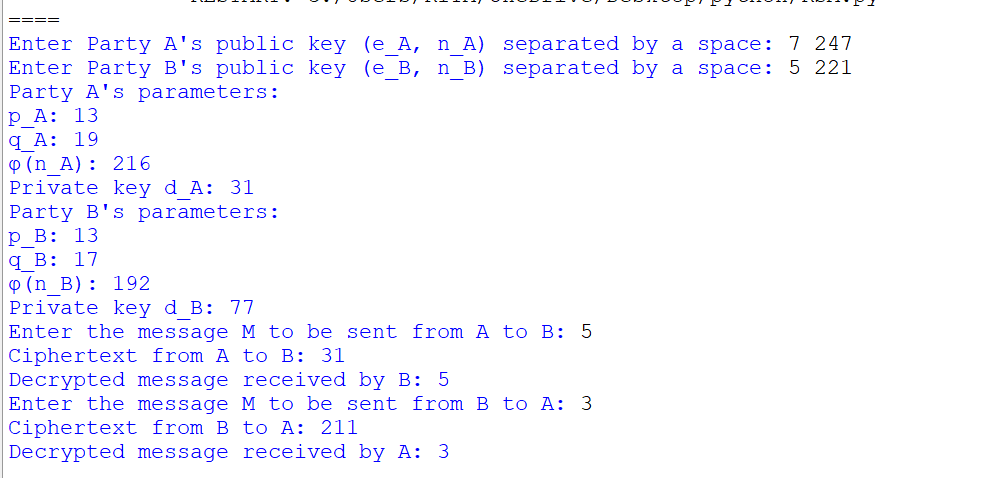
# A decrypts the message

decrypted\_message\_A = rsa\_decrypt(ciphertext\_B\_to\_A, d\_A, n\_A)

print(f"Decrypted message received by A: {decrypted\_message\_A}")

**Output:**

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